

Introduction to Mathematical Software Exercise 2



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Problem 1 plot and plot3d

a) Let

$$f(x) = \sin(\pi \cdot x^3),$$

$$g(x) = e^{-x^2}.$$

Plot $f(x)$ and $g(x)$ with $x \in [-2, 2]$. Get familiar with the `plots`-package. Try to plot f and g into one picture.

b) Plot $h(x) = x^2$ and its derivative from $x = 0$ to ∞ . Enjoy the result!

c) How can you plot the function $\text{MonkeySaddle}(x, y) = x^3 - 3 \cdot x \cdot y^2$, $x \in [-2, 2]$, $y \in [-2, 2]$? Take a look into Maple's help in order to find out more about plotting.

Problem 2 Lists and Sets in Maple

a) Explain the difference between lists and sets in Maple.

b) Use Maple to find the common divisors of 23545800, 25491186 and 229420674. *Hint*: How can the package `numtheory` help you?

c) Let Maple evaluate the function `sin` for all solutions of the equation

$$x^4 - 4 \cdot x^3 \cdot \pi + \frac{26}{9} \cdot x^2 \cdot \pi^2 + \frac{4}{9} \cdot x \cdot \pi^3 - \frac{1}{3} \cdot \pi^4 = 0$$

by using `solve` and

i) `map`,

ii) the element-wise operator `~` (only if you are using Maple 14, as this is not implemented in Maple 11).

Problem 3 Solving Systems of Linear Equations

Try to solve the following systems of linear equations. What is happening?

$$2 \cdot x + 8 \cdot y + 4 \cdot z = 7$$

$$6 \cdot x + 2 \cdot y + 4 \cdot z = 9$$

$$x + z = 8$$

$$2 \cdot x + 8 \cdot y + 4 \cdot z = 7$$

$$6 \cdot x + 2 \cdot y + 4 \cdot z = 9$$

$$2 \cdot x + 8 \cdot y + 4 \cdot z = 7$$

$$6 \cdot x + 2 \cdot y + 4 \cdot z = 9$$

$$3 \cdot x + 8 \cdot y + 5 \cdot z = 15$$

$$x + z = 8$$

$$2 \cdot x + 8 \cdot y + 4 \cdot z = 7$$

$$6 \cdot x + 2 \cdot y + 4 \cdot z = 9$$

$$3 \cdot x + 8 \cdot y + 5 \cdot z = 9$$

$$x + z = 8$$

Problem 4 Curve Sketching

Let

$$f(x) = \frac{x^2 + 5 \cdot x - 12}{2 \cdot x^2 - 12 \cdot x + 16}.$$

- Plot $f(x)$ for $x \in [-10, 10]$. Use the same Interval as range of your plot. Have a look at help topic `plot/options` in order to find out how to do that. Also try to find out how to avoid ugly discontinuities in your plot.
- Find the domain [DEFINITIONSBEREICH] of f .
- Find the zeros [NULLSTELLEN] of f .
- Find local minima and maxima of f .
- Find inflection points [WENDEPUNKTE] of f .
- Calculate the area under the graph between the first two zeros (there should be at least two zeros).

Don't Drink and Derive – Episode 1

Two math professors are sitting in a pub.

“Isn't it disgusting”, the first one complains, “how little the general public knows about mathematics?”

“Well”, his colleague replies, “you're perhaps a bit too pessimistic.”

“I don't think so”, the first one replies. “And anyhow, I have to go to the washroom now.”

He goes off, and the other professor decides to use this opportunity to play a prank on his colleague. He makes a sign to the pretty, blonde waitress to come over.

“When my friend comes back, I'll wave you over to our table, and I'll ask you a question. I would like you to answer: x to the third over three. Can you do that?”

“Sure.” The girl giggles and repeats several times: “ x to the third over three, x to the third over three, x to the third over three...”

When the first professor comes back from the washroom, his colleague says: “I still think, you're way too pessimistic. I'm sure the waitress knows a lot more about mathematics than you imagine.”

He makes her come over and asks her: “Can you tell us what the integral of x squared is?”

She replies: “ x to the third over three.”

The other professor's mouth drops wide open, and his colleague grins smugly when the waitress adds: “...plus C .”