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**Algorithm 9:** Bipartite Matching

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**Input:** undirected bipartite graph  $G = (S \cup T, E)$

**Output:** maximal matching  $M$

// Construct a flow network:

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1  $V \leftarrow S \cup T \cup \{s, t\}$ 
2  $A_1 \leftarrow \{(s, v) \mid v \in S\}$ 
3  $A_2 \leftarrow \{(v, w) \mid \{v, w\} \in E\}$ 
4  $A_3 \leftarrow \{(w, t) \mid w \in T\}$ 
5  $A \leftarrow A_1 \cup A_2 \cup A_3$ 
6  $D \leftarrow (V, A)$ 
7 foreach  $a \in A$  do
8   |  $c(a) \leftarrow 1$ 
   // Use Edmonds-Karp:
9  $f \leftarrow$  maximal flow on  $(D, s, t, c)$ 
   // Find the matching:
10  $M \leftarrow \emptyset$ 
11 foreach  $a \in A_2$  do
12   | if  $f(a) > 0$  then
13   | |  $M \leftarrow M \cup \{a\}$ 
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