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**Method 7: Ford-Fulkerson**

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**Input:** directed graph  $G = (V, E)$ , capacity

$c : E \rightarrow \mathbb{R}_{\geq 0}$ , source  $s \in V$ , sink  $t \in V$

**Output:** maximal flow  $f : E \rightarrow \mathbb{R}_{\geq 0}$ , flow value  $f_{\max}$

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1  $f_{\max} \leftarrow 0$ 
2 foreach  $e = (u, v) \in E$  do
3   |  $c_f(v, u) \leftarrow 0$ 
4 foreach  $e = (u, v) \in E$  do
5   |  $c_f(e) \leftarrow c(e)$ 
6  $E_f \leftarrow E$ 
7 while there is an  $(s - t)$ -path  $p$  in  $G_f = (V, E_f)$  do
8   |  $c_p \leftarrow \min\{c_f(e) \mid e \in p\}$ 
9   |  $f_{\max} \leftarrow f_{\max} + c_p$ 
10  foreach  $(u, v) \in p$  do
11    |  $c_f(u, v) \leftarrow c_f(u, v) - c_p$ 
12    |  $c_f(v, u) \leftarrow c_f(v, u) + c_p$ 
13    | if  $c_f(u, v) = 0$  then
14      |   remove  $(u, v)$  from  $E_f$ 
15    | if  $(v, u) \notin E_f$  then
16      |   add  $(v, u)$  to  $E_f$ 
17 foreach  $e \in E$  do
18   |  $f(e) \leftarrow c(e) - c_f(e)$ 
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