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**Algorithm 3:** Kruskal's Algorithm

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**Input:** graph  $G = (V, E)$ , weight function  $w : E \rightarrow \mathbb{R}$

**Output:** minimal spanning tree  $T = (V, F)$  of  $G$

```
1  $F \leftarrow \emptyset$ 
2  $L \leftarrow E$ 
3 Sort the edges in  $L$  increasingly by weight
4 while  $L \neq \emptyset$  do
5   |  $e \leftarrow \text{pop\_front}(L)$ 
6   | if  $(V, F \cup \{e\})$  is acyclic then
7   | |  $F \leftarrow F \cup \{e\}$ 
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**Algorithm 4:** Prim's Algorithm

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**Input:** connected graph  $G = (V, E)$  given as adjacency list, weight function  $w : E \rightarrow \mathbb{R}$ , root node  $r \in V$

**Output:** minimal spanning tree

$T = (V, \{(v, \text{pred}(v)) \mid v \in V \setminus \{r\}\})$  of  $G$

```
1 foreach  $v \in V$  do
2   |    $\text{pred}(v) \leftarrow 0$ 
3   |    $\text{dist}(v) \leftarrow \infty$  // distance from tree
4  $Q \leftarrow V$  // priority queue
5  $\text{dist}(r) \leftarrow 0$ 
6 while  $Q \neq \emptyset$  do
7   |    $v \leftarrow \text{extract\_min}(Q)$  // vertex with minimal
8       |   distance
9       |   foreach  $u \in \text{Adj}(v)$  do
10      |   |   if  $u \in Q$  and  $w(u, v) < \text{dist}(u)$  then
11      |   |   |    $\text{pred}(u) \leftarrow v$ 
11      |   |   |    $\text{dist}(u) \leftarrow w(u, v)$ 
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