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**Algorithm 12:** MergeSort( $A, \ell, u$ )

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**Input:** array  $A = (a_0, \dots, a_{n-1})$ ,  $\ell, u$

```
1 if  $\ell < u$  then
2   |    $m \leftarrow \lceil \frac{u-\ell}{2} \rceil$ 
3   |   MergeSort( $A, \ell, m - 1$ )
4   |   MergeSort( $A, m, u$ )
5   |   Merge( $A, \ell, u, m$ )
```

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**Function** Merge( $A, \ell, u, m$ )

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**Input:** array  $A = (a_0, \dots, a_{n-1})$ ,  $\ell, u, m$

```
1  $n_1 \leftarrow m - \ell, n_2 \leftarrow u - m + 1$ 
2  $L \leftarrow$  array of length  $n_1 + 1, U \leftarrow$  array of length  $n_2 + 1$ 
3 for  $i \leftarrow 0, \dots, n_1 - 1$  do
4   |    $L[i] \leftarrow A[\ell + i]$ 
5 for  $i \leftarrow 0, \dots, n_2 - 1$  do
6   |    $U[i] \leftarrow A[m + i]$ 
7  $L[n_1] \leftarrow \infty, U[n_2] \leftarrow \infty$ 
8  $i \leftarrow 0, j \leftarrow 0$ 
9 for  $k \leftarrow \ell, \dots, u$  do
10  |   if  $L[i] \leq U[j]$  then
11  |   |    $A[k] \leftarrow L[i]$ 
12  |   |    $i \leftarrow i + 1$ 
13  |   else
14  |   |    $A[k] \leftarrow U[j]$ 
15  |   |    $j \leftarrow j + 1$ 
```

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To sort an array  $A = (a_0, \dots, a_{n-1})$ , call

MergeSort( $A, 0, n - 1$ ).