
Algorithm 1: Breadth-First-Search (BFS)

Input: graph $G = (V, E)$, $V = \{1, \dots, n\}$ given as
adjacency list, root node $r \in V$

Output: level function $L : V \rightarrow \mathbb{Z}_{\geq 0} \cup \{\infty\}$,
predecessor function $\text{pred} : V \rightarrow V \cup \{0\}$

```
1 foreach  $v \in V \setminus \{r\}$  do
2    $L(v) \leftarrow \infty$ 
3    $\text{pred}(v) \leftarrow 0$ 
4    $\text{seen}(v) \leftarrow 0$ 
5    $L(r) \leftarrow 0$ 
6    $\text{pred}(r) \leftarrow 0$ 
7    $\text{seen}(r) \leftarrow 1$ 
8    $Q \leftarrow \emptyset$ 
9    $\text{push\_back}(Q, r)$ 
10  while  $Q \neq \emptyset$  do
11     $u \leftarrow \text{pop\_front}(Q)$ 
12    foreach  $v \in \text{Adj}(u)$  do
13      if  $\text{seen}(v) = 0$  then
14         $\text{seen}(v) \leftarrow 1$ 
15         $L(v) \leftarrow L(u) + 1$ 
16         $\text{pred}(v) \leftarrow u$ 
17         $\text{push\_back}(Q, v)$ 
```

Algorithm 2: Depth-First-Search (DFS)

Input: graph $G = (V, E)$, $V = \{1, \dots, n\}$ given as adjacency list

Output: predecessor function $\text{pred} : V \rightarrow V \cup \{0\}$

```
1 foreach  $v \in V$  do
2   | pred( $v$ )  $\leftarrow 0$ 
3   | seen( $v$ )  $\leftarrow 0$ 
4 foreach  $v \in V$  do
5   | if seen( $v$ ) = 0 then
6     |   | DFSvisit( $G, v$ )
```

Function DFSvisit(G, r)

Input: graph $G = (V, E)$ given as adjacency list, root node $r \in V$

```
1 seen( $r$ )  $\leftarrow 1$ 
2 foreach  $v \in \text{Adj}(r)$  do
3   | if seen( $v$ ) = 0 then
4     |   | pred( $v$ ) =  $r$ 
5     |   | DFSvisit( $G, v$ )
```
